

LONG-RANGE PLAN

Junior Division: Grades 4-6, Mathematics

Organized by Topics

What is a long-range plan and why is it important?

A long-range plan outlines a year-long plan for learning mathematics. It is a living document that is revised as educators become increasingly aware of the abilities, strengths, needs and interests of their students. A thoughtfully developed long-range plan:

- ensures that instruction is sequenced in a manner that aligns with research about learning mathematics;
- allocates the appropriate time for concepts and skills so that students have multiple opportunities to focus on the overall expectations within the grade;
- ensures that all specific expectations are addressed at least once within the school year; and
- recognizes that some expectations need to be revisited several times throughout the year.

Note: These sample long-range plans outline possible sequences of instruction for the school year. There are many ways to structure an effective plan for learning.

How are these long-range plans structured?

Deep learning occurs when specific expectations are connected, are continuously expanded upon, and are revisited in a variety of contexts throughout the year.

This long-range plan is structured into learning clusters or topics to support students in making connections within a cluster of specific expectations. Topics are carefully ordered to create a flow of learning to strengthen student understanding. In turn, learning can be expanded and applied in subsequent topics.

Suggested timing for each topic is specified, but there should be room for flexibility. Educators should make adjustments to timing if additional days are required to address student learning needs that emerge as the plan is implemented.



Considerations

- Sample long-range plans for each grade level include all overall and specific expectations from strands B through F.
- The overall expectation from Strand A (Social-Emotional Learning Skills and the Mathematical Processes) is integrated and taught in connection with the other strands throughout the school year.
- In developing long-range and daily plans, consider opportunities to teach
 and reinforce social-emotional learning skills and mathematical processes,
 as well as transferable skills, in order to help students develop confidence,
 cope with challenges, think critically and creatively, and develop a positive
 identity as a math learner.
- Mathematical modelling (Algebra, C4) provides opportunities for students
 to authentically engage in learning with everyday situations that involve
 mathematics. Tasks that require the process of mathematical modelling
 can be strategically situated throughout the year to support students in
 making connections among mathematical concepts, strands, and
 disciplines, and to provide opportunities for assessing the integration and
 application of learning.
- Coding (Algebra, C3) can be used to solve problems and help deepen students' understanding of mathematical concepts; it is strategically addressed and assessed throughout the year, as appropriate.
- Some concepts and skills require ongoing attention so that students can
 develop proficiency and deep, lasting learning. Number Talks, Number
 Strings, and other math talk prompts can be used at the beginning of math
 classes to reinforce and strengthen number relationships, spatial
 relationships, math facts, mental math strategies, and problem-solving
 skills.

Reflective questions when planning

- What key concepts, models, and strategies do students need more time to develop?
- Does the long-range plan revisit expectations later? If not, how might I adjust the plan so it does? What prior learning is assumed in order for other expectations to be addressed?
- How can I create opportunities for students to continue to practise and consolidate learning when they are engaged in new learning?



Long-Range Plan: Junior Division (Grades 4-6)

The Social-Emotional Learning (SEL) Skills and the Mathematical Processes are to be integrated throughout each of the topics below as appropriate.

Grade 4	Grade 5	Grade 6	
Numbers, Patterns & Shapes in Everyday Life (10 days)	Numbers, Patterns & Shapes in Everyday Life (10 days)	Numbers, Patterns & Shapes in Everyday Life (10 days)	
Number, Algebra, Spatial Sense	Number, Algebra, Spatial Sense	Number, Algebra, Spatial Sense	
Facts, Expressions & Equations including the Area of Rectangles (10 days) Number, Algebra, Spatial Sense	Facts, Expressions & Equations including the Area of Parallelograms & Triangles (10 days) Number, Algebra, Spatial Sense	including Area of Various Shapes (10 days)	
Number, Atgebra, Spanat Sense	Number, Atgebra, Spatial Sense	Number, Algebra, Spatial Sense	
Number Patterns & Number Relationships (10 days)	Number Patterns & Number Relationships (10 days)	Number Patterns & Number Relationships (10 days)	
Number, Algebra	Number, Algebra	Number, Algebra	
Data & Introduction to Mathematical Modelling (30 days)	Data & Introduction to Mathematical Modelling (30 days)	Data & Introduction to Mathematical Modelling (30 days)	
Number, Algebra. Data	Number. Algebra Data	Number. Algebra, Data	
Transformations & Coding	Transformations & Coding	Transformations & Coding	
Algebra, Spatial Sense	Algebra, Spatial Sense	Algebra, Spatial Sense	
Comparison of Measures, Quantities & Expressions (10 days)	Comparison of Measures, Quantities & Expressions (10 days)	Comparison of Measures, Quantities & Expressions (10 days)	
Number, Algebra, Spatial Sense	Number, Algebra, Spatial Sense	Number, Algebra, Spatial Sense	
Proportional Relationships & Measurement (10 days)	Proportional Relationships & Measurement (10 days)	Proportional Relationships & Operations with Fractions (10 days)	
Number, Spatial Sense	Number, Spatial Sense, Financial Literacy	Number	
Patterns & Likelihood of Events (15 days)	Patterns & Probability	Patterns & Probability (15 days)	
Algebra, Data, Spatial Sense	Algebra, Data, Spatial Sense	Algebra, Data	
Operations & Measurement	Operations & Measurement	Operations & Measurement	
Number, Spatial Sense	Number, Algebra, Spatial Sense	Number, Algebra, Spatial Sense	
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Financial Literacy & Operations involving Money (10 days) Number, Algebra, Financial Literacy	Financial Literacy & Operations involving Money (10 days) Number, Algebra, Financial Literacy	Financial Literacy & Operations involving Money (10 days) Number, Algebra, Financial Literacy
Integrated Task (10 days) Algebra	Integrated Task (10 days) Algebra	Integrated Task (10 days) Algebra



Grade 4 Long-Range Plan

155 days + 35 days discretionary

NOTE: The **Social-Emotional Learning Skills** and the **Mathematical Processes** are introduced, applied, and integrated throughout the year as appropriate.

Time	Topics and Expectations			
10 days	Attributes and Numbers			
days	Introd	luce and apply throughout the year as appropriate		
	B1.1	read, represent, compose, and decompose whole numbers up to and including 10 000, using appropriate tools and strategies, and describe various ways they are used in everyday life		
	B1.7	read, represent, compare, and order decimal tenths, in various contexts		
	E2.3	solve problems involving elapsed time by applying the relationships between different units of time		
	Using	characteristics to classify		
	C1.1	identify and describe repeating and growing patterns, including patterns found in real- life contexts		
	E1.1	identify geometric properties of rectangles, including the number of right angles, parallel and perpendicular sides, and lines of symmetry		
	E2.4	identify angles and classify them as right, straight, acute, or obtuse		
10	Facts	s, Expressions and Equations including Area of a Rectangle		
days	Dovol	aning multiplication facts using the area of a rectangle		
	B2.2	loping multiplication facts using the area of a rectangle recall and demonstrate multiplication facts for 1 × 1 to 10 × 10, and related division facts		
	E2.5	use the row and column structure of an array to measure the areas of rectangles and		
	L2.5	to show that the area of any rectangle can be found by multiplying its side lengths		
	Unde	rstanding and working with equations		
	B2.1	use the properties of operations, and the relationships between addition, subtraction, multiplication, and division, to solve problems involving whole numbers, including those requiring more than one operation, and check calculations		
	C2.1	identify and use symbols as variables in expressions and equations		
	C2.2	solve equations that involve whole numbers up to 50 in various contexts, and verify solutions		
	E2.6	apply the formula for the area of a rectangle to find the unknown measurement when given two of the three		
10	Number Patterns and Number Relationships			
days	Exten	Extending place value to decimal tenths		
	B1.1	read, represent, compose, and decompose whole numbers up to and including 10 000, using appropriate tools and strategies, and describe various ways they are used in everyday life		
	B1.6	count to 10 by halves, thirds, fourths, fifths, sixths, eighths, and tenths, with and without the use of tools		
	C1.4	create and describe patterns to illustrate relationships among whole numbers and decimal tenths		

Representing fractions

- B1.4 represent fractions from halves to tenths using drawings, tools, and standard fractional notation, and explain the meanings of the denominator and the numerator
- B1.9 describe relationships and show equivalences among fractions and decimal tenths, in various contexts
- B2.7 represent the relationship between the repeated addition of a unit fraction and the multiplication of that unit fraction by a whole number, using tools, drawings, and standard fractional notation

30 days

Collection, Organization, Representation, and Analysis of Data, and Introduction to Mathematical Modelling

Collecting, organizing, and representing data

- B1.1 read, represent, compose, and decompose whole numbers up to and including 10 000, using appropriate tools and strategies, and describe various ways they are used in everyday life
- B1.2 compare and order whole numbers up to and including 10 000, in various contexts
- D1.1 describe the difference between qualitative and quantitative data, and describe situations where each would be used
- D1.2 collect data from different primary and secondary sources to answer questions of interest that involve comparing two or more sets of data, and organize the data in frequency tables and stem-and-leaf plots
- D1.3 select from among a variety of graphs, including multiple-bar graphs, the type of graph best suited to represent various sets of data; display the data in the graphs with proper sources, titles, and labels, and appropriate scales; and justify their choice of graphs
- D1.4 create an infographic about a data set, representing the data in appropriate ways, including in frequency tables, stem-and-leaf plots, and multiple-bar graphs, and incorporating any other relevant information that helps to tell a story about the data

Analysing data using mean, median, and mode

- B2.1 use the properties of operations, and the relationships between addition, subtraction, multiplication, and division, to solve problems involving whole numbers, including those requiring more than one operation, and check calculations
- D1.5 determine the mean and the median and identify the mode(s), if any, for various data sets involving whole numbers, and explain what each of these measures indicates about the data
- D1.6 analyse different sets of data presented in various ways, including in stem-and-leaf plots and multiple-bar graphs, by asking and answering questions about the data and drawing conclusions, then make convincing arguments and informed decisions
- D2.2 make and test predictions about the likelihood that the mean, median, and mode(s) of a data set will be the same for data collected from different populations

Posing a real-life situation that requires the process of mathematical modelling and involves the collection, organization, representation and analysis of data.*

- C4 apply the process of mathematical modelling to represent, analyse, make predictions, and provide insight into real-life situations**
- Depending on the situation it may be appropriate to complete the mathematical modelling task now or continue as new learning is acquired
- "One aspect of the mathematical modelling process is to identify things that change (variable) and things that remain the same

Transformations and Coding

Creating, describing, and performing transformations

- E1.3 describe and perform translations and reflections on a grid, and predict the results of these transformations
- E1.2 plot and read coordinates in the first quadrant of a Cartesian plane, and describe the translations that move a point from one coordinate to another
- C3.1 solve problems and create computational representations of mathematical situations by writing and executing code, including code that involves sequential, concurrent, repeating, and nested events
- C3.2 read and alter existing code, including code that involves sequential, concurrent, repeating, and nested events, and describe how changes to the code affect the outcomes

10 days

Comparison of Quantities

Comparing measures

E2.2 use metric prefixes to describe the relative size of different metric units, and choose appropriate units and tools to measure length, mass, and capacity

Comparing whole numbers, fractions and decimal tenths

- B1.2 compare and order whole numbers up to and including 10 000, in various contexts
- B1.5 use drawings and models to represent, compare, and order fractions representing the individual portions that result from two different fair-share scenarios involving any combination of 2, 3, 4, 5, 6, 8, and 10 sharers
- B1.7 read, represent, compare, and order decimal tenths, in various contexts

Comparing two expressions

C2.3 solve inequalities that involve addition and subtraction of whole numbers up to 20, and verify and graph the solutions

10 days

Proportional Relationships and Measurements

Using proportional reasoning

- B2.3 use mental math strategies to multiply whole numbers by 10, 100, and 1000, divide whole numbers by 10, and add and subtract decimal tenths, and explain the strategies used
- E2.1 explain the relationships between grams and kilograms as metric units of mass, and between litres and millilitres as metric units of capacity, and use benchmarks for these units to estimate mass and capacity
- E2.2 use metric prefixes to describe the relative size of different metric units, and choose appropriate units and tools to measure length, mass, and capacity
- B2.8 show simple multiplicative relationships involving whole-number rates, using various tools and drawings
- E2.3 solve problems involving elapsed time by applying the relationships between different units of time



Patterns and Likelihood of Events

Creating patterns and code, and making predictions about them

- C1.2 create and translate repeating and growing patterns using various representations, including tables of values and graphs
- C1.3 determine pattern rules and use them to extend patterns, make and justify predictions, and identify missing elements in repeating and growing patterns
- C3.1 solve problems and create computational representations of mathematical situations by writing and executing code, including code that involves sequential, concurrent, repeating, and nested events
- C3.2 read and alter existing code, including code that involves sequential, concurrent, repeating, and nested events, and describe how changes to the code affect the outcomes

Predicting the likelihood of an event

D2.1 use mathematical language, including the terms "impossible", "unlikely", "equally likely", "likely", and "certain", to describe the likelihood of events happening, represent this likelihood on a probability line, and use it to make predictions and informed decisions

30 days

Operations

Developing fluency with adding, subtracting, multiplying, and dividing

- B1.8 round decimal numbers to the nearest whole number, in various contexts
- B2.4 represent and solve problems involving the addition and subtraction of whole numbers that add up to no more than 10 000 and of decimal tenths, using appropriate tools and strategies, including algorithms
- B2.5 represent and solve problems involving the multiplication of two- or three-digit whole numbers by one-digit whole numbers and by 10, 100, and 1000, using appropriate tools, including arrays
- B2.6 represent and solve problems involving the division of two- or three-digit whole numbers by one-digit whole numbers, expressing any remainder as a fraction when appropriate, using appropriate tools, including arrays

10 days

Financial Literacy and Operations involving Money

Developing financial concepts

- F1.3 explain the concepts of spending, saving, earning, investing, and donating, and identify key factors to consider when making basic decisions related to each
- F1.4 explain the relationship between spending and saving, and describe how spending and saving behaviours may differ from one person to another
- F1.5 describe some ways of determining whether something is reasonably priced and therefore a good purchase
- F1.1 identify various methods of payment that can be used to purchase goods and services

Using operations and mental math to solve problems involving purchases

- F1.2 estimate and calculate the cost of transactions involving multiple items priced in whole-dollar amounts, not including sales tax, and the amount of change needed when payment is made in cash, using mental math
- B1.3 round whole numbers to the nearest ten, hundred, or thousand, in various contexts
- B2.1 use the properties of operations, and the relationships between addition, subtraction, multiplication, and division, to solve problems involving whole numbers, including those requiring more than one operation, and check calculations
- C3.1 solve problems and create computational representations of mathematical situations by writing and executing code, including code that involves conditional statements and other control structures
- C3.2 read and alter existing code, including code that involves conditional statements and other control structures, and describe how changes to the code affect the outcomes

Integrated Task

This is an opportunity to apply mathematical concepts and skills from this grade to solve real-life problems that require the process of mathematical modelling*.

Depending on the real-life situation, coding may be a tool in mathematical modelling

- C3.1 solve problems and create computational representations of mathematical situations by writing and executing code, including code that involves conditional statements and other control structures
- C3.2 read and alter existing code, including code that involves conditional statements and other control structures, and describe how changes to the code affect the outcomes
- One aspect of the mathematical modelling process is to identify things that change (variable) and things that remain the same. Variables may be used to represent quantities that will change.



Grade 5 Long-Range Plan

155 days + 35 days discretionary

NOTE: The **Social-Emotional Learning Skills** and the **Mathematical Processes** are introduced, applied, and integrated throughout the year as appropriate.

Time	Topics and Expectations			
10 days	Attributes and Numbers			
aays	Introduce and apply throughout the year as appropriate			
	B2.2	recall and demonstrate multiplication facts from 0 × 0 to 12 × 12, and related division facts		
	B2.3	use mental math strategies to multiply whole numbers by 0.1 and 0.01 and estimate sums and differences of decimal numbers up to hundredths, and explain the strategies used		
	Exten	ding place value to 100 000 and decimal hundredths		
	B1.1	read, represent, compose, and decompose whole numbers up to and including 100 000, using appropriate tools and strategies, and describe various ways they are used in everyday life		
	B1.5	read, represent, compare, and order decimal numbers up to hundredths, in various contexts		
	C1.4	create and describe patterns to illustrate relationships among whole numbers and decimal tenths and hundredths		
	Using	characteristics to classify		
	C1.1	identify and describe repeating, growing, and shrinking patterns, including patterns found in real-life contexts		
	E1.1	identify geometric properties of triangles, and construct different types of triangles when given side or angle measurements		
10 days	Facts Trian	s, Expressions and Equations including the Area of Parallelograms and igles		
	Devel	oping multiplication facts using the area of a rectangles,		
	B2.2	recall and demonstrate multiplication facts from 0 × 0 to 12 × 12, and related division facts		
	E2.5	use the area relationships among rectangles, parallelograms, and triangles to develop the formulas for the area of a parallelogram and the area of a triangle, and solve related problems		
	E2.6	show that two-dimensional shapes with the same area can have different perimeters, and solve related problems		
	Unde	rstanding and working with expressions and equations		
	B2.1	use the properties of operations, and the relationships between operations, to solve problems involving whole numbers and decimal numbers, including those requiring more than one operation, and check calculations		
	C2.1	translate among words, algebraic expressions, and visual representations that describe equivalent relationships		
	C2.3	solve equations that involve whole numbers up to 100 in various contexts, and verify solutions		
	C2.2	evaluate algebraic expressions that involve whole numbers		

Number Patterns and Number Relationships

Representing fractions and showing equivalences to decimals and percents

- B1.3 represent equivalent fractions from halves to twelfths, including improper fractions and mixed numbers, using appropriate tools, in various contexts
- B1.7 describe relationships and show equivalences among fractions, decimal numbers up to hundredths, and whole number percents, using appropriate tools and drawings, in various contexts
- B2.5 add and subtract fractions with like denominators, in various contexts

30 days

Collection, Organization, Representation, and Analysis of Data, and Introduction to Mathematical Modelling

Collecting, organizing, and representing data

- B1.7 describe relationships and show equivalences among fractions, decimal numbers up to hundredths, and whole number percents, using appropriate tools and drawings, in various contexts
- D1.1 explain the importance of various sampling techniques for collecting a sample of data that is representative of a population
- D1.2 collect data, using appropriate sampling techniques as needed, to answer questions of interest about a population, and organize the data in relative-frequency tables
- D1.3 select from among a variety of graphs, including stacked-bar graphs, the type of graph best suited to represent various sets of data; display the data in the graphs with proper sources, titles, and labels, and appropriate scales; and justify their choice of graphs
- D1.4 create an infographic about a data set, representing the data in appropriate ways, including in relative-frequency tables and stacked-bar graphs, and incorporating any other relevant information that helps to tell a story about the data

Analysing data using mean, median, and mode

- D1.5 determine the mean and the median and identify the mode(s), if any, for various data sets involving whole numbers and decimal numbers, and explain what each of these measures indicates about the data
- D1.6 analyse different sets of data presented in various ways, including in stacked-bar graphs and in misleading graphs, by asking and answering questions about the data, challenging preconceived notions, and drawing conclusions, then make convincing arguments and informed decisions

Posing a real-life situation that requires the process of mathematical modelling and involves the collection, organization, representation and analysis of data.*

- C4 apply the process of mathematical modelling to represent, analyse, make predictions, and provide insight into real-life situations**
- Depending on the situation it may be appropriate to complete the mathematical modelling task now or continue as new learning is acquired
- ** One aspect of the mathematical modelling process is to identify things that change (variable) and things that remain the same

10 days

Transformations and Coding

Creating, describing, and performing transformations

- E1.5 describe and perform translations, reflections, and rotations up to 180 on a grid, and predict the results of these transformations
- E1.4 plot and read coordinates in the first quadrant of a Cartesian plane using various scales, and describe the translations that move a point from one coordinate to another
- C3.1 solve problems and create computational representations of mathematical situations by writing and executing code, including code that involves conditional statements and other control structures
- C3.2 read and alter existing code, including code that involves conditional statements and other control structures, and describe how changes to the code affect the outcomes



Comparison of Measures, Quantities and Expressions

Comparing measures

- E2.1 use appropriate metric units to estimate and measure length, area, mass, and capacity
- E2.3 compare angles and determine their relative size by matching them and by measuring them using appropriate non-standard units
- E2.4 explain how protractors work, use them to measure and construct angles up to 180, and use benchmark angles to estimate the size of other angles
- E1.2 identify and construct congruent triangles, rectangles, and parallelograms

Comparing whole numbers, fractions and decimal tenths

- B1.2 compare and order whole numbers up to and including 100 000, in various contexts
- B1.4 compare and order fractions from halves to twelfths, including improper fractions and mixed numbers, in various contexts
- B1.5 read, represent, compare, and order decimal numbers up to hundredths, in various contexts
- E2.2 solve problems that involve converting larger metric units into smaller ones, and describe the base ten relationships among metric units

Comparing two expressions

C2.4 solve inequalities that involve one operation and whole numbers up to 50, and verify and graph the solutions

10 days

Proportional Relationships and Measurements

Using proportional reasoning

- B2.3 use mental math strategies to multiply whole numbers by 0.1 and 0.01 and estimate sums and differences of decimal numbers up to hundredths, and explain the strategies used
- E2.2 solve problems that involve converting larger metric units into smaller ones, and describe the base ten relationships among metric units
- B2.9 represent and create equivalent ratios and rates, using a variety of tools and models, in various contexts
- F1.5 calculate unit rates for various goods and services, and identify which rates offer the best value

15 days

Patterns and Probability

Creating patterns and code, and making predictions about them

- C1.1 identify and describe repeating, growing, and shrinking patterns, including patterns found in real-life contexts
- C1.2 create and translate growing and shrinking patterns using various representations, including tables of values and graphs
- C1.3 determine pattern rules and use them to extend patterns, make and justify predictions, and identify missing elements in repeating, growing, and shrinking patterns
- C3.1 solve problems and create computational representations of mathematical situations by writing and executing code, including code that involves conditional statements and other control structures
- C3.2 read and alter existing code, including code that involves conditional statements and other control structures, and describe how changes to the code affect the outcomes

Expressing and predicting probability

- D2.1 use fractions to express the probability of events happening, represent this probability on a probability line, and use it to make predictions and informed decisions
- D2.2 determine and compare the theoretical and experimental probabilities of an event happening



Operations and Measurement

Developing fluency with adding, subtracting, multiplying, and dividing

- B1.6 round decimal numbers to the nearest tenth, in various contexts
- B2.1 use the properties of operations, and the relationships between operations, to solve problems involving whole numbers and decimal numbers, including those requiring more than one operation, and check calculations
- B2.4 represent and solve problems involving the addition and subtraction of whole numbers that add up to no more than 100 000, and of decimal numbers up to hundredths, using appropriate tools, strategies, and algorithms
- B2.6 represent and solve problems involving the multiplication of two-digit whole numbers by two-digit whole numbers using the area model and using algorithms, and make connections between the two methods
- B2.7 represent and solve problems involving the division of three-digit whole numbers by two-digit whole numbers using the area model and using algorithms, and make connections between the two methods, while expressing any remainder appropriately
- B2.5 add and subtract fractions with like denominators, in various contexts
- B2.8 multiply and divide one-digit whole numbers by unit fractions, using appropriate tools and drawings

Understanding and working with expressions and equations

- C2.1 translate among words, algebraic expressions, and visual representations that describe equivalent relationships
- C2.2 evaluate algebraic expressions that involve whole numbers

10 days

Financial Literacy and Operations involving Money

Developing financial concepts

- F1.1 describe several ways money can be transferred among individuals, organizations, and businesses
- F1.3 design sample basic budgets to manage finances for various earning and spending scenarios
- F1.4 explain the concepts of credit and debt, and describe how financial decisions may be impacted by each
- F1.6 describe the types of taxes that are collected by the different levels of government in Canada, and explain how tax revenue is used to provide services in the community

Using operations and mental math to solve problems involving purchases

- F1.2 estimate and calculate the cost of transactions involving multiple items priced in dollars and cents, including sales tax, using various strategies
- B2.1 use the properties of operations, and the relationships between operations, to solve problems involving whole numbers and decimal numbers, including those requiring more than one operation, and check calculations
- C3.1 solve problems and create computational representations of mathematical situations by writing and executing code, including code that involves conditional statements and other control structures
- C3.2 read and alter existing code, including code that involves conditional statements and other control structures, and describe how changes to the code affect the outcomes

Integrated Task

This is an opportunity to apply mathematical concepts and skills from this grade to solve real-life problems that require the process of mathematical modelling*.

Depending on the real-life situation, coding may be a tool in mathematical modelling

- C3.1 solve problems and create computational representations of mathematical situations by writing and executing code, including code that involves conditional statements and other control structures
- C3.2 read and alter existing code, including code that involves conditional statements and other control structures, and describe how changes to the code affect the outcomes
- One aspect of the mathematical modelling process is to identify things that change (variable) and things that remain the same. Variables may be used to represent quantities that will change.

Grade 6 Long-Range Plan

155 days + 35 days discretionary

NOTE: The **Social-Emotional Learning Skills** and the **Mathematical Processes** are introduced, applied, and integrated throughout the year as appropriate.

Time	Topics and Expectations			
10	Attributes and Numbers, Patterns and Shapes in Everyday Life			
days	Extending place value to one million and decimal thousandths			
	B1.1	read and represent whole numbers up to and including one million, using appropriate tools and strategies, and describe various ways they are used in everyday life		
	C1.4	create and describe patterns to illustrate relationships among whole numbers and decimal numbers		
	Using	characteristics to classify		
	C1.1	identify and describe repeating, growing, and shrinking patterns, including patterns found in real-life contexts, and specify which growing patterns are linear		
	E1.1	create lists of the geometric properties of various types of quadrilaterals, including the properties of the diagonals, rotational symmetry, and line symmetry		
	Deter	mining area by decomposing shapes		
	E2.4	determine the areas of trapezoids, rhombuses, kites, and composite polygons by decomposing them into shapes with known areas		
	E2.5	create and use nets to demonstrate the relationship between the faces of prisms and pyramids and their surface areas		
	E2.6	determine the surface areas of prisms and pyramids by calculating the areas of their two-dimensional faces and adding them together		
10	Facts	s, Expressions and Equations including Area of Various Shapes		
days	Apply	addition facts to add monomials		
	C2.1	add monomials with a degree of 1 that involve whole numbers, using tools		
	Under	standing and working with expressions and equations		
	B2.1	use the properties of operations, and the relationships between operations, to solve problems involving whole numbers, decimal numbers, fractions, ratios, rates, and whole number percents, including those requiring multiple steps or multiple operations		
	C2.2	evaluate algebraic expressions that involve whole numbers and decimal tenths		
	C2.3	solve equations that involve multiple terms and whole numbers in various contexts, and verify solutions		

Number Patterns and Number Relationships

Finding factors

- B2.2 understand the divisibility rules and use them to determine whether numbers are divisible by 2, 3, 4, 5, 6, 8, 9, and 10
- B2.6 represent composite numbers as a product of their prime factors, including through the use of factor trees
- B1.5 round decimal numbers, both terminating and repeating, to the nearest tenth, hundredth, or whole number, as applicable, in various contexts

Working with integers

- B1.2 read and represent integers, using a variety of tools and strategies, including horizontal and vertical number lines
- B1.3 compare and order integers, decimal numbers, and fractions, separately and in combination, in various contexts
- E1.3 plot and read coordinates in all four quadrants of a Cartesian plane, and describe the translations that move a point from one coordinate to another

25 days

Collection, Organization, Representation, and Analysis of Data, and Introduction to Mathematical Modelling

Collecting, organizing, and representing data

- D1.1 describe the difference between discrete and continuous data, and provide examples of each
- D1.2 collect qualitative data and discrete and continuous quantitative data to answer questions of interest about a population, and organize the sets of data as appropriate, including using intervals
- D1.3 select from among a variety of graphs, including histograms and broken-line graphs, the type of graph best suited to represent various sets of data; display the data in the graphs with proper sources, titles, and labels, and appropriate scales; and justify their choice of graphs
- D1.4 create an infographic about a data set, representing the data in appropriate ways, including in tables, histograms, and broken-line graphs, and incorporating any other relevant information that helps to tell a story about the data

Analysing data using measures of central tendency

- D1.5 determine the range as a measure of spread and the measures of central tendency for various data sets, and use this information to compare two or more data sets
- D1.6 analyse different sets of data presented in various ways, including in histograms and broken-line graphs and in misleading graphs, by asking and answering questions about the data, challenging preconceived notions, and drawing conclusions, then make convincing arguments and informed decisions

Posing a real-life situation that requires the process of mathematical modelling and involves the collection, organization, representation and analysis of data.*

- C4 apply the process of mathematical modelling to represent, analyse, make predictions, and provide insight into real-life situations**
- Depending on the situation it may be appropriate to complete the mathematical modelling task now or continue as new learning is acquired
- One aspect of the mathematical modelling process is to identify things that change (variable) and things that remain the same



Transformations and Coding

Creating, describing, and performing transformations

- E1.4 describe and perform combinations of translations, reflections, and rotations up to 360 on a grid, and predict the results of these transformations
- E1.3 plot and read coordinates in all four quadrants of a Cartesian plane, and describe the translations that move a point from one coordinate to another
- C3.1 solve problems and create computational representations of mathematical situations by writing and executing efficient code, including code that involves conditional statements and other control structures
- C3.2 read and alter existing code, including code that involves conditional statements and other control structures, and describe how changes to the code affect the outcomes and the efficiency of the code

15 days

Comparison of Measures, Quantities and Expressions

Comparing measures spatially

- E1.2 construct three-dimensional objects when given their top, front, and side views
- E2.5 create and use nets to demonstrate the relationship between the faces of prisms and pyramids and their surface areas
- E2.6 determine the surface areas of prisms and pyramids by calculating the areas of their two-dimensional faces and adding them together

Comparing measures using standard units

- E2.2 use a protractor to measure and construct angles up to 360, and state the relationship between angles that are measured clockwise and those that are measured counterclockwise
- E2.3 use the properties of supplementary angles, complementary angles, opposite angles, and interior and exterior angles to solve for unknown angle measures
- E2.1 measure length, area, mass, and capacity using the appropriate metric units, and solve problems that require converting smaller units to larger ones and vice versa

Comparing integers, fractions, and decimal numbers

- B1.4 read, represent, compare, and order decimal numbers up to thousandths, in various contexts
- B1.3 compare and order integers, decimal numbers, and fractions, separately and in combination, in various contexts
- B1.6 describe relationships and show equivalences among fractions and decimal numbers up to thousandths, using appropriate tools and drawings, in various contexts

Comparing two expressions

C2.4 solve inequalities that involve two operations and whole numbers up to 100, and verify and graph the solutions

10 days

Proportional Relationships and Operations with Fractions

Using proportional reasoning

- B2.3 use mental math strategies to calculate percents of whole numbers, including 1%, 5%, 10%, 15%, 25%, and 50%, and explain the strategies used
- B2.12 solve problems involving ratios, including percents and rates, using appropriate tools and strategies
- B2.5 add and subtract fractions with like and unlike denominators, using appropriate tools, in various contexts
- B2.9 multiply whole numbers by proper fractions, using appropriate tools and strategies
- B2.10 divide whole numbers by proper fractions, using appropriate tools and strategies



Patterns and Probability

Creating patterns and code, and making predictions about them

- C1.1 identify and describe repeating, growing, and shrinking patterns, including patterns found in real-life contexts, and specify which growing patterns are linear
- C1.2 create and translate repeating, growing, and shrinking patterns using various representations, including tables of values, graphs, and, for linear growing patterns, algebraic expressions and equations
- C1.3 determine pattern rules and use them to extend patterns, make and justify predictions, and identify missing elements in repeating, growing, and shrinking patterns, and use algebraic representations of the pattern rules to solve for unknown values in linear growing patterns
- C2.3 solve equations that involve multiple terms and whole numbers in various contexts, and verify solutions

NOTE: solving for an unknown value with an algebraic representation of a pattern is an application in solving equations

Expressing and predicting probability

- D2.1 use fractions, decimals, and percents to express the probability of events happening, represent this probability on a probability line, and use it to make predictions and informed decisions
- D2.2 determine and compare the theoretical and experimental probabilities of two independent events happening

Coding can be used to create patterns, check predictions, and simulate probabilities

- C3.1 solve problems and create computational representations of mathematical situations by writing and executing efficient code, including code that involves conditional statements and other control structures
- C3.2 read and alter existing code, including code that involves conditional statements and other control structures, and describe how changes to the code affect the outcomes and the efficiency of the code

30 days

Operations and Measurement

Developing fluency with adding, subtracting, multiplying, and dividing

- B2.1 use the properties of operations, and the relationships between operations, to solve problems involving whole numbers, decimal numbers, fractions, ratios, rates, and whole number percents, including those requiring multiple steps or multiple operations
- B2.4 represent and solve problems involving the addition and subtraction of whole numbers and decimal numbers, using estimation and algorithms
- B2.7 represent and solve problems involving the multiplication of three-digit whole numbers by decimal tenths, using algorithms
- B2.8 represent and solve problems involving the division of three-digit whole numbers by decimal tenths, using appropriate tools, strategies, and algorithms, and expressing remainders as appropriate
- B2.11 represent and solve problems involving the division of decimal numbers up to thousandths by whole numbers up to 10, using appropriate tools and strategies
- C2.2 evaluate algebraic expressions that involve whole numbers and decimal tenths

Financial Literacy and Operations involving Money

Developing financial concepts

- F1.1 describe the advantages and disadvantages of various methods of payment that can be used to purchase goods and services
- F1.2 identify different types of financial goals, including earning and saving goals, and outline some key steps in achieving them
- F1.3 identify and describe various factors that may help or interfere with reaching financial goals
- F1.4 explain the concept of interest rates, and identify types of interest rates and fees associated with different accounts and loans offered by various banks and other financial institutions
- F1.5 describe trading, lending, borrowing, and donating as different ways to distribute financial and other resources among individuals and organizations

Using operations and mental math to solve problems involving purchases

- B2.1 use the properties of operations, and the relationships between operations, to solve problems involving whole numbers, decimal numbers, fractions, ratios, rates, and whole number percents, including those requiring multiple steps or multiple operations
- C3.1 solve problems and create computational representations of mathematical situations by writing and executing efficient code, including code that involves conditional statements and other control structures
- C3.2 read and alter existing code, including code that involves conditional statements and other control structures, and describe how changes to the code affect the outcomes and the efficiency of the code

10 days

Integrated Task

This is an opportunity to apply mathematical concepts and skills from this grade to solve real-life problems that require the process of mathematical modelling*.

Depending on the real-life situation, coding may be a tool in mathematical modelling

- C3.1 solve problems and create computational representations of mathematical situations by writing and executing efficient code, including code that involves conditional statements and other control structures
- C3.2 read and alter existing code, including code that involves conditional statements and other control structures, and describe how changes to the code affect the outcomes and the efficiency of the code
- * One aspect of the mathematical modelling process is to identify things that change (variable) and things that remain the same. Variables may be used to represent quantities that will change.

