

Loads

LRFD Brace axial force	$P_u := 840\text{kip}$
horizontal nodal force	$H_{u_{\text{node}}} := 100\text{kip}$
beam axial reaction	$A_{u_{\text{beam}}} := 716\text{kip}$
beam shear reaction	$V_{u_{\text{beam}}} := 50\text{kip}$

Material Properties

Beams steel grade A992	$F_{y_{\text{beam}}} := 50\text{-ksi}$	$F_{u_{\text{beam}}} := 65\text{-ksi}$
Brace steel grade A36	$F_{y_{\text{brace}}} := 36\text{-ksi}$	$F_{u_{\text{brace}}} := 58\text{-ksi}$
Plate steel grade A572 Gr. 50	$F_{y_{\text{PL}}} := 50\text{ksi}$	$F_{u_{\text{PL}}} := 65\text{ksi}$
Modulus of Elasticity	$E := 29000\text{ksi}$	
weld strength	$F_{\text{EXX}} := 70\text{ksi}$	

Member Properties**Beam Properties**

Beam section	$\text{Beam} := \text{"W21X83"}$	$\text{Span} := 25\text{ft}$
depth of beam	$d_{\text{beam}} := T1(\text{Row}(\text{Beam}), 7) \cdot \text{in} = 21.4 \cdot \text{in}$	
width of flange	$b_{f_{\text{beam}}} := T1(\text{Row}(\text{Beam}), 12) \cdot \text{in} = 8.4 \cdot \text{in}$	
thickness of flange	$t_{f_{\text{beam}}} := T1(\text{Row}(\text{Beam}), 20) \cdot \text{in} = 0.835 \cdot \text{in}$	
thickness of web	$t_{w_{\text{beam}}} := T1(\text{Row}(\text{Beam}), 17) \cdot \text{in} = 0.515 \cdot \text{in}$	
design weld depth	$k_{\text{des}_{\text{brace}}} := T1(\text{Row}(\text{Beam}), 25) \cdot \text{in} = 1.34 \cdot \text{in}$	
center of web to flange toe of fillet	$k_{1_{\text{beam}}} := T1(\text{Row}(\text{Beam}), 27) \cdot \text{in} = 0.875 \cdot \text{in}$	
strong moment of inertia	$I_{x_{\text{beam}}} := T1(\text{Row}(\text{Beam}), 39) \cdot \text{in}^4 = 1830 \cdot \text{in}^4$	

Column Properties

	$\text{Column} := \text{"W14X90"}$
depth	$d_{\text{column}} := T1(\text{Row}(\text{Column}), 7) \cdot \text{in} = 14 \cdot \text{in}$
flange width	$b_{f_{\text{column}}} := T1(\text{Row}(\text{Column}), 12) \cdot \text{in} = 14.5 \cdot \text{in}$
flange thickness	$t_{f_{\text{column}}} := T1(\text{Row}(\text{Column}), 20) \cdot \text{in} = 0.71 \cdot \text{in}$
web thickness	$t_{w_{\text{column}}} := T1(\text{Row}(\text{Column}), 17) \cdot \text{in} = 0.44 \cdot \text{in}$
strong moment of inertia	$I_{x_{\text{column}}} := T1(\text{Row}(\text{Column}), 39) \cdot \text{in}^4 = 999 \cdot \text{in}^4$

Brace Properties

Brace section	$\text{Brace} := "2L8X6X1LLBB"$	
cross sectional area	$A_{g_{\text{brace}}} := T1(\text{Row}(\text{Brace}), 6) \cdot \text{in}^2 = 26.2 \cdot \text{in}^2$	
x distance to centroid	$x_{\text{bar}}_{\text{brace}} := T1(\text{Row}(L1), 28) \cdot \text{in} = 1.65 \cdot \text{in}$	$L1 := "L8X6X1"$ value for single angle
	$t_{\text{brace}} := T1(\text{Row}(\text{Brace}), 22) \cdot \text{in} = 1 \text{ in}$	

Plate Properties

thickness	$t_{\text{PL}} := 1 \text{ in}$
clip thickness	$t_{\text{clip}} := \frac{3}{4} \text{ in}$
end PL width	$h_{\text{endPL}} := 10 \text{ in}$

Member DesignBrace-to-Gusset ConnectionDetermine required number of bolts (J3.6)

bolt pitch (spacing)	$p := 3 \text{ in}$	
bolt diameter	$d_{\text{bolt}} := \frac{7}{8} \text{ in}$	
area of bolt	$A_{\text{bolt}} := d_{\text{bolt}}^2 \cdot \frac{\pi}{4} = 0.6 \text{ in}^2$	
bolt shear strength	$F_{nv_{\text{bolt}}} := 84 \text{ ksi}$	Table J3.2 Group A threads X
bolt tensile strength	$F_{nt_{\text{bolt}}} := 113 \text{ ksi}$	
strength reduction factor	$\Phi := 0.75$	
bolt shear strength (single shear)	$\Phi_{r_{nv}} := \Phi F_{nv_{\text{bolt}}} A_{\text{bolt}} = 37.9 \text{ kip}$	EQ : J3-1
bolt tensile strength	$\Phi_{r_{nt}} := \Phi F_{nt_{\text{bolt}}} A_{\text{bolt}} = 51 \text{ kip}$	EQ : J3-1
number of bolts	$N_{\text{bolts}} := \frac{P_u}{\Phi_{r_{nv}} \cdot (2)} = 11.1$	use 14 bolts $N_{\text{bolts}} := 14$
double shear		recall $P_u = 840 \text{ kip}$

Check tensile yielding on the brace gross section (J4.1a)

strength reduction factor	$\Phi := 0.9$
tensile yielding strength of brace	$\Phi R_n := \Phi \cdot F_{y_{brace}} \cdot A_{g_{brace}} = 848.9 \text{ kip}$
check capacity	$\text{if}(P_u < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$

recall

$F_{y_{brace}} = 36 \text{ ksi}$
$A_{g_{brace}} = 26.2 \text{ in}^2$
$P_u = 840 \text{ kip}$

Check tensile rupture on the brace net section (J4.1b)

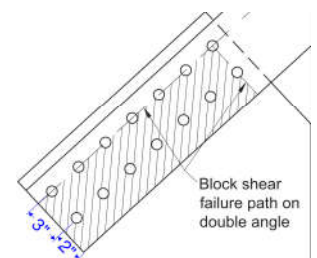
net area of brace	$A_{n_{brace}} := A_{g_{brace}} - 4 \cdot t_{brace} \cdot \left(d_{bolt} + \frac{2}{16} \text{ in} \right) = 22.2 \text{ in}^2$
length of bolted connection	$l_{brace} := \left(\frac{14}{2} - 1 \right) \cdot 3 \text{ in} = 18 \text{ in}$
shear lag factor (Tbl D3.1 case 2)	$U := 1 - \frac{x_{bar_{brace}}}{l_{brace}} = 0.908$
effective area of brace	$A_{e_{brace}} := U \cdot A_{n_{brace}} = 20.2 \text{ in}^2$
strength reduction factor	$\Phi := 0.75$
tensile rupture strength of brace	$\Phi R_n := \Phi \cdot F_{u_{brace}} \cdot A_{e_{brace}} = 877.2 \text{ kip}$
check capacity	$\text{if}(P_u < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$

recall

$A_{g_{brace}} = 26.2 \text{ in}^2$
$t_{brace} = 1 \text{ in}$
$x_{bar_{brace}} = 1.65 \text{ in}$
$F_{y_{brace}} = 36 \text{ ksi}$
$F_{u_{brace}} = 58 \text{ ksi}$
$F_{y_{PL}} = 50 \text{ ksi}$
$F_{u_{PL}} = 65 \text{ ksi}$
$N_{bolts} = 14$
$d_{bolt} = 0.875 \text{ in}$
$p = 3 \text{ in}$
$t_{PL} = 1 \text{ in}$
$P_u = 840 \text{ kip}$

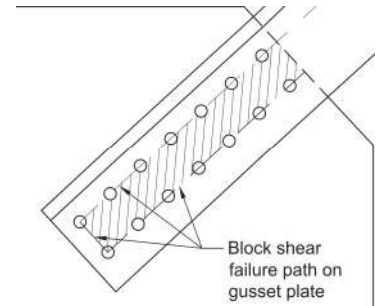
Check block shear rupture on the brace (J4.3)

block shear strength	$R_n = 0.60 F_u \cdot A_{nv} + U_{bs} \cdot F_u \cdot A_{nt} \leq 0.60 F_y \cdot A_{gv} + U_{bs} \cdot F_u \cdot A_{nt}$
gross shear area	$A_{gv_{brace}} := (2) \cdot t_{brace} \cdot (l_{brace} + 1.5 \text{ in}) = 39 \text{ in}^2$
net area for shear	$A_{nv_{brace}} := A_{gv_{brace}} - (2) \cdot \left(\frac{14}{2} - 0.5 \right) \cdot t_{brace} \cdot \left(d_{bolt} + \frac{2}{16} \text{ in} \right) = 26 \text{ in}^2$
net area for tension	$A_{nt_{brace}} := (2) \cdot t_{brace} \cdot \left[(p + 2 \text{ in}) - 1.5 \cdot \left(d_{bolt} + \frac{2}{16} \text{ in} \right) \right] = 7 \text{ in}^2$
uniformly loaded	$U_{bs} := 1$
strength reduction factor	$\Phi := 0.75$
block shear strength	$\Phi R_n := \Phi \cdot (0.6 \min(F_{u_{brace}} \cdot A_{nv_{brace}}, F_{y_{brace}} \cdot A_{gv_{brace}}) + U_{bs} \cdot F_{u_{brace}} \cdot A_{nt_{brace}})$ $\Phi R_n = 936.3 \text{ kip}$
check capacity	$\text{if}(P_u < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$



Check block shear rupture on the gusset plate (J4.3)

gross shear area	$A_{gv_{PL}} := 2 \cdot t_{PL} \cdot (l_{brace} + 1.5 \text{ in}) = 39 \text{ in}^2$	
net area for shear	$A_{nv_{PL}} := A_{gv_{PL}} - (2) \left(\frac{14}{2} - 0.5 \right) \cdot t_{PL} \cdot \left(d_{bolt} + \frac{2}{16} \text{ in} \right)$	
	$A_{nv_{PL}} = 26 \text{ in}^2$	
net area for tension	$A_{nt_{PL}} := t_{PL} \cdot \left[3 \text{ in} - \left(d_{bolt} + \frac{2}{16} \text{ in} \right) \right] = 2 \text{ in}^2$	$0.60 F_{u_{PL}} \cdot A_{nv_{PL}} = 1014 \text{ kip}$
uniformly loaded	$U_{bs} := 1$	$0.60 F_{y_{PL}} \cdot A_{gv_{PL}} = 1170 \text{ kip}$
strength reduction factor	$\Phi := 0.75$	$U_{bs} \cdot F_{u_{PL}} \cdot A_{nt_{PL}} = 130 \text{ kip}$
block shear strength	$\Phi R_n := \Phi \cdot (0.6 \min(F_{u_{PL}} \cdot A_{nv_{PL}}, F_{y_{PL}} \cdot A_{gv_{PL}}) + U_{bs} \cdot F_{u_{PL}} \cdot A_{nt_{PL}}) = 858 \text{ kip}$	
check capacity	$\text{if}(P_u < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$	

Check bolt bearing on the gusset plate (J3.10)

bolt bearing strength	$R_n = 1.2 \cdot l_c \cdot t \cdot F_u < 2.4 \cdot d \cdot t \cdot F_u$	<u>recall</u> $\Phi r_{nv} = 37.9 \text{ kip}$
clear distance (between bolts)	$l_{c_inner} := 3 \text{ in} - \left(d_{bolt} + \frac{1}{16} \text{ in} \right) = 2.06 \text{ in}$	$d_{bolt} = 0.875 \text{ in}$
clear distance (between edge)	$l_{c_edge} := 1.5 \text{ in} - 0.5 \cdot \left(d_{bolt} + \frac{1}{16} \text{ in} \right) = 1.03 \text{ in}$	$F_{u_{PL}} = 65 \text{ ksi}$
		$N_{bolts} = 14$
		$P_u = 840 \text{ kip}$
strength reduction factor	$\Phi := 0.75$	
edge bolt bearing strength	$\Phi R_{n_edge} := \min[\Phi \cdot 1.2 \cdot l_{c_edge} \cdot t_{PL} \cdot F_{u_{PL}}, \Phi \cdot 2.4 \cdot d_{bolt} \cdot t_{PL} \cdot F_{u_{PL}}, (2) \Phi r_{nv}] = 60.3 \text{ kip}$	
inner bolt bearing strength	$\Phi R_{n_inner} := \min[\Phi \cdot 1.2 \cdot l_{c_inner} \cdot t_{PL} \cdot F_{u_{PL}}, \Phi \cdot 2.4 \cdot d_{bolt} \cdot t_{PL} \cdot F_{u_{PL}}, (2) \Phi r_{nv}] = 75.8 \text{ kip}$	
Total bolt bearing strength	$\Phi R_n := (2) \cdot \Phi R_{n_edge} + (N_{bolts} - 2) \cdot \Phi R_{n_inner} = 1029.9 \text{ kip}$	
check capacity	$\text{if}(P_u < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$	

Check the gusset plate for tensile yielding on the Whitmore section (pg: 9-3)

whitmore section width	$l_w := p + \tan(30 \text{ deg}) \cdot 2 \cdot l_{brace} = 23.8 \text{ in}$	<u>recall</u> $l_{brace} = 18 \text{ in}$
	$l_{w_web} := 4.70 \text{ in}$	$tw_{beam} = 0.515 \text{ in}$
effective area of the Whitmore section	$A_w := (l_w - l_{w_web}) \cdot t_{PL} + (l_{w_web}) \cdot tw_{beam} = 21.5 \text{ in}^2$	$t_{PL} = 1 \text{ in}$
		$F_{y_{PL}} = 50 \text{ ksi}$
		$P_u = 840 \text{ kip}$

tensile yielding strength of the gusset plate (J4.1a)

strength reduction factor	$\Phi := 0.90$
tensile yielding strength	$\Phi R_n := \Phi \cdot F_{yPL} \cdot A_w = 967.7 \text{ kip}$
check capacity	$\text{if}(P_u < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$

Check the gusset plate for compression buckling on the Whitmore section (J4.4)

effective length factor	$K_{PL} := 0.5$
length of plate to buckle	$L_{PL} := 9.76 \text{ in}$
radius of gyration	$r_{PL} := \sqrt{\frac{L_{PL} \cdot t_{PL}^3}{12 \cdot t_{PL} \cdot L_{PL}}} = 0.289 \text{ in}$
$\frac{K \cdot L}{r}$	$\frac{K_{PL} \cdot L_{PL}}{r_{PL}} = 16.9 < 25$

recall

$t_{PL} = 1 \text{ in}$
$F_{yPL} = 50 \text{ ksi}$
$P_u = 840 \text{ kip}$

gross area	$A_{gPL} := t_{PL} \cdot 20.9 \text{ in} = 20.9 \text{ in}^2$
strength reduction factor	$\Phi := 0.90$
compressive strength	$\Phi P_n := \Phi \cdot F_{yPL} \cdot A_{gPL} = 940.5 \text{ kip}$
check capacity	$\text{if}(P_u < \Phi P_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$

Connection Interface Forces (chapter 13)

beam half depth	$e_{\text{beam}} := \frac{d_{\text{beam}}}{2} = 10.7 \text{ in}$	<u>recall</u>
column half depth	$e_{\text{column}} := \frac{d_{\text{column}}}{2} = 7 \text{ in}$	$d_{\text{beam}} = 21.4 \text{ in}$
slope of brace	$\theta_{\text{brace}} := \text{atan}\left(\frac{12}{11.125}\right) = 47.2 \cdot \text{deg}$	$d_{\text{column}} = 14 \text{ in}$
	$\alpha - \beta \cdot \tan(\theta) = e_{\text{beam}} \cdot \tan(\theta) - e_{\text{column}}$	$P_u = 840 \text{ kip}$
	$\beta_{\text{bar}} := 12 \text{ in}$	
	$\beta := \beta_{\text{bar}}$	
	$\alpha := e_{\text{beam}} \cdot \tan(\theta_{\text{brace}}) - e_{\text{column}} + \beta \cdot \tan(\theta_{\text{brace}}) = 17.5 \text{ in}$	Eq : 13-1
plate thickness	$t_p := 1 \text{ in}$	

$$\alpha_{\text{bar}} = \alpha = \frac{l_h + t_{\text{clip}}}{2} + t_p$$

$$l_h := 2(\alpha - t_p) - t_{\text{clip}} = 32.2 \text{ in}$$

$$r := \sqrt{(\alpha + e_{\text{column}})^2 + (\beta + e_{\text{beam}})^2} = 33.4 \text{ in} \quad \text{Eq. 13-6}$$

$$V_{\text{column}} := \frac{\beta}{r} \cdot P_u = 301.9 \text{ kip} \quad \text{Eq. 13-2}$$

$$V_{\text{beam}} := \frac{e_{\text{beam}}}{r} \cdot P_u = 269.2 \text{ kip} \quad \text{Eq. 13-4}$$

$$P_u \cdot \cos(\theta_{\text{brace}}) - (V_{\text{column}} + V_{\text{beam}}) = -0 \text{ kip}$$

$$H_{\text{column}} := \frac{e_{\text{column}}}{r} \cdot P_u = 176.1 \text{ kip} \quad \text{Eq. 13-3}$$

$$H_{\text{beam}} := \frac{\alpha}{r} \cdot P_u = 439.9 \text{ kip} \quad \text{Eq. 13-5}$$

$$P_u \cdot \sin(\theta_{\text{brace}}) - (H_{\text{column}} + H_{\text{beam}}) = -0 \text{ kip}$$

Gusset-to-Beam Connection

Check gusset plate for shear yielding (J4.2a) and tensile yielding (J4.1a) along the beam flange

weld length	$l_{\text{weld}} := l_h - 0.75 \text{ in} = 31.5 \text{ in}$	<u>recall</u>
strength reduction factor	$\Phi := 1.00$	$l_h = 32.2 \text{ in}$
shear yielding strength	$\Phi R_n := \Phi \cdot 0.60 \cdot F_{YPL} \cdot t_{PL} \cdot l_{\text{weld}} = 944.1 \text{ kip}$	$t_{PL} = 1 \text{ in}$
check capacity	$\text{if}(H_{\text{beam}} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$	$F_{YPL} = 50 \text{ ksi}$
strength reduction factor	$\Phi := 0.90$	$H_{\text{beam}} = 439.9 \text{ kip}$
Tensile yielding strength	$\Phi R_n := \Phi \cdot F_{YPL} \cdot t_{PL} \cdot l_{\text{weld}} = 1416.2 \text{ kip}$	$V_{\text{beam}} = 269.2 \text{ kip}$
check capacity	$\text{if}(V_{\text{beam}} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$	

Consider force interaction for gusset plate

interaction Eq plasticity theory
(Neal, 1977) and suggested by
Astaneh-Asl (1998)

$$\left(\frac{M_{ub}}{\Phi M_n}\right) + \left(\frac{V_{ub}}{\Phi N_n}\right)^2 + \left(\frac{H_{ub}}{\Phi V_n}\right)^4 < 1$$

recall

strength reduction factor

$$\Phi := 0.90$$

$$\Phi M_{n_{PL}} = \Phi \cdot F_y \cdot Z_x$$

$$F_{y_{PL}} = 50 \text{ ksi}$$

$$l_{weld} = 31.5 \text{ in}$$

$$t_{PL} = 1 \text{ in}$$

nominal moment strength (EQ: F2-1)

$$\Phi M_{n_{PL}} := \Phi \cdot F_{y_{PL}} \cdot \left(\frac{t_{PL} \cdot l_{weld}^2}{4}\right) = 11142.1 \text{ in} \cdot \text{kip}$$

$$H_{beam} = 439.9 \text{ kip}$$

$$V_{beam} = 269.2 \text{ kip}$$

interaction equation

$$\left(\frac{0}{\Phi M_{n_{PL}}}\right) + \left[\frac{V_{beam}}{0.90 \cdot (F_{y_{PL}} \cdot t_{PL} \cdot l_{weld})}\right]^2 + \left[\frac{H_{beam}}{1.0 \cdot (0.60 \cdot F_{y_{PL}} \cdot t_{PL} \cdot l_{weld})}\right]^4 = 0.08$$

Design weld at gusset-to-beam flange connection

axial stress in weld

$$f_a := \frac{V_{beam}}{l_{weld}} = 8.6 \cdot \frac{\text{kip}}{\text{in}}$$

recall

$$l_{weld} = 31.5 \text{ in}$$

$$H_{beam} = 439.9 \text{ kip}$$

shear stress in weld

$$f_v := \frac{H_{beam}}{l_{weld}} = 14 \cdot \frac{\text{kip}}{\text{in}}$$

$$V_{beam} = 269.2 \text{ kip}$$

bending stress in weld

$$f_b := 0$$

peak stress

$$f_{peak} := \sqrt{(f_a + f_b)^2 + f_v^2} = 16.4 \cdot \frac{\text{kip}}{\text{in}}$$

average stress

$$f_{avg} := \frac{1}{2} \cdot \left[\sqrt{(f_a - f_b)^2 + f_v^2} + \sqrt{(f_a + f_b)^2 + f_v^2} \right] = 16.4 \cdot \frac{\text{kip}}{\text{in}}$$

load angle

$$\theta_{load} := \text{atan}\left(\frac{f_a}{f_v}\right) = 31.5 \cdot \text{deg}$$

additional ductility (pg: 13-11)

$$\text{ductility} := 1.25$$

stress on weld

$$f_{weld} := \max(\text{ductility} \cdot f_{avg}, f_{peak}) = 20.5 \cdot \frac{\text{kip}}{\text{in}}$$

gusset to beam flange weld size

$$D := \frac{f_{weld}}{2 \cdot \left(1.392 \frac{\text{kip}}{\text{in}}\right) \cdot \left(1.0 + 0.50 \cdot \sin(\theta_{load})^{1.5}\right)} = 6.2$$

$$D := \text{ceil}(D) \cdot \text{in} = 7 \text{ in} \quad 16 \text{ th of an inch}$$

Check beam web local yielding (J10.2)

strength reduction factor

$$\Phi := 1.00$$

web local yielding strength

$$\Phi R_n = \Phi \cdot F_{yw} \cdot t_w \cdot (2.5k + l_b)$$

check capacity

$$\Phi R_n := \Phi \cdot F_{ybeam} \cdot t_{wbeam} \cdot (2.5k_{desbrace} + l_{weld}) = 896.6 \text{ kip}$$

$$\text{if}(V_{beam} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$F_{ybeam} = 50 \text{ ksi}$$

$$t_{wbeam} = 0.5 \text{ in}$$

$$k_{desbrace} = 1.3 \text{ in}$$

$$l_{weld} = 31.5 \text{ in}$$

$$V_{beam} = 269.2 \text{ kip}$$

Check equivalent normal force, Ne

$$N_{ue} := V_{beam} + \frac{2 \cdot 0}{(l_{weld} \div 2)} = 269.2 \text{ kip}$$

recall

$$t_{wbeam} = 0.5 \text{ in}$$

$$l_{weld} = 31.5 \text{ in}$$

$$d_{beam} = 21.4 \text{ in}$$

recall

$$t_{fbeam} = 0.84 \text{ in}$$

$$F_{ybeam} = 50 \text{ ksi}$$

$$E = 29000 \text{ ksi}$$

$$V_{beam} = 269.2 \text{ kip}$$

Check beam web local crippling (J10.3)

strength reduction factor

$$\Phi := 0.75$$

web local crippling strength

$$\Phi R_n := \Phi \cdot 0.80 \cdot t_{wbeam}^2 \cdot \left[1 + 3 \cdot \left(\frac{l_{weld}}{d_{beam}} \right) \cdot \left(\frac{t_{wbeam}}{t_{fbeam}} \right)^{1.5} \right] \cdot \sqrt{\frac{E \cdot F_{ybeam} \cdot t_{fbeam}}{t_{wbeam}}} = 765.4 \text{ kip}$$

check capacity

$$\text{if}(V_{beam} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Gusset-to-Column ConnectionDesign bolts at gusset-to-column connection (J3.6 & J3.7)

number of bolts

$$N_{bolts.end_PL} := 14$$

ultimate shear force per bolt

$$r_{uv} := \frac{V_{column}}{N_{bolts.end_PL}} = 21.6 \text{ kip}$$

check capacity

$$\text{if}(r_{uv} < \Phi r_{nv}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

ultimate tensile force per bolt

$$r_{ut} := \frac{H_{column}}{N_{bolts.end_PL}} = 12.6 \text{ kip}$$

check capacity

$$\text{if}(r_{ut} < \Phi r_{nt}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$F_{nvbolt} = 84 \text{ ksi}$$

$$F_{ntbolt} = 113 \text{ ksi}$$

$$\Phi r_{nv} = 37.9 \text{ kip}$$

$$\Phi r_{nt} = 51 \text{ kip}$$

$$H_{column} = 176.1 \text{ kip}$$

$$V_{column} = 301.9 \text{ kip}$$

$$A_{bolt} = 0.6 \text{ in}^2$$

strength reduction factor

$$\Phi := 0.75$$

modified nominal tensile stress factored to include shear stress effects

$$F'_{nt} = 1.3 \cdot F_{nt} - \frac{F_{nt}}{\Phi \cdot F_{nv}} \cdot r_{rv} < F_{nt}$$

$$F'_{ntbolt} := \min \left[1.3 \cdot F_{ntbolt} - \frac{F_{ntbolt}}{\Phi \cdot F_{nvbolt}} \cdot \left(\frac{r_{uv}}{A_{bolt}} \right), F_{ntbolt} \right] = 82.6 \text{ ksi}$$

combined loading strength

$$\Phi R_n := \Phi \cdot F'_{ntbolt} \cdot A_{bolt} = 37.2 \text{ kip}$$

check capacity

$$\text{if}(r_{ut} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Design gusset-to-end plate weld (Eq: 8-2)

resultant load on weld

$$R_u := \sqrt{H_{\text{column}}^2 + V_{\text{column}}^2} = 349.5 \text{ kip}$$

resultant weld load angle

$$\theta_{\text{resultant}} := \text{atan}\left(\frac{H_{\text{column}}}{V_{\text{column}}}\right) = 30.3 \cdot \text{deg}$$

end plate effective length of weld

$$l_{\text{weld.end_PL}} := p \cdot \frac{N_{\text{bolts.end_PL}}}{2} = 21 \text{ in}$$

end plate weld size

$$D_{\text{end_PL}} := \frac{R_u}{(2) \cdot \left(1.392 \frac{\text{kip}}{\text{in}}\right) \cdot l_{\text{weld.end_PL}} \cdot \left(1.0 + 0.50 \cdot \sin(\theta_{\text{resultant}})\right)^{1.5}} = 5.1$$

$$D_{\text{end_PL}} := \text{ceil}(D_{\text{end_PL}}) = 6$$

recall

$$H_{\text{column}} = 176.1 \text{ kip}$$

$$V_{\text{column}} = 301.9 \text{ kip}$$

$$N_{\text{bolts.end_PL}} = 14$$

$$p = 3 \text{ in}$$

Check gusset plate tensile and shear yielding at the gusset-to-end-plate interface (J4.1a & J4.2a)

strength reduction factor

$$\Phi := 0.90$$

Tensile yielding strength

$$\Phi N_n := \Phi \cdot F_{yPL} \cdot (t_{PL} \cdot l_w) = 1070.3 \text{ kip}$$

check capacity

$$\text{if}(H_{\text{column}} < \Phi N_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

strength reduction factor

$$\Phi := 1.00$$

shear yielding strength

$$\Phi V_n := \Phi \cdot 0.60 \cdot F_{yPL} \cdot (t_{PL} \cdot l_w) = 713.5 \text{ kip}$$

check capacity

$$\text{if}(V_{\text{column}} < \Phi V_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$l_w = 23.8 \text{ in}$$

$$t_{PL} = 1 \text{ in}$$

$$F_{yPL} = 50 \text{ ksi}$$

$$H_{\text{column}} = 176.1 \text{ kip}$$

$$V_{\text{column}} = 301.9 \text{ kip}$$

Check prying action on bolts at the end plate (Part 9 and Figure 5-4a)

bolt gage

$$\text{gage} := 5.5 \text{ in}$$

$$b_{\text{endPL}} := \frac{\text{gage} - t_{PL}}{2} = 2.3 \text{ in}$$

Eq 9-21

$$b'_{\text{endPL}} := b_{\text{endPL}} - \frac{d_{\text{bolt}}}{2} = 1.8 \text{ in}$$

Eq 9-27

$$a_{\text{endPL}} := \frac{h_{\text{endPL}} - \text{gage}}{2} = 2.25 \text{ in}$$

$$a'_{\text{endPL}} := \min\left(a_{\text{endPL}} + \frac{d_{\text{bolt}}}{2}, 1.25 \cdot b_{\text{endPL}} + \frac{d_{\text{bolt}}}{2}\right) = 2.69 \text{ in}$$

$$\rho_{\text{endPL}} := \frac{b'_{\text{endPL}}}{a'_{\text{endPL}}} = 0.674$$

$$d' := d_{\text{bolt}} + \frac{1}{16} \text{ in} = \frac{15}{16} \text{ in}$$

Eq 9-24

$$\delta_{\text{endPL}} := 1 - \frac{d'}{p} = 0.69$$

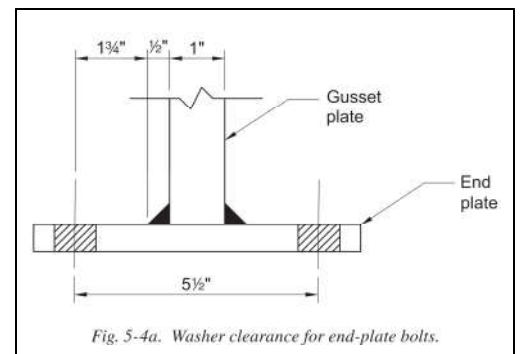


Fig. 5-4a. Washer clearance for end-plate bolts.

recall

$$t_{PL} = 1 \text{ in}$$

$$d_{\text{bolt}} = \frac{7}{8} \text{ in}$$

$$h_{\text{endPL}} = 10 \text{ in}$$

$$\Phi r_{nt} = 51 \text{ kip}$$

$$p = 3 \text{ in}$$

$$\Phi r_{nt} = 51 \text{ kip}$$

$$F_{uPL} = 65 \text{ ksi}$$

$$r_{ut} = 12.6 \text{ kip}$$

available tensile bolt strength

$$B := \Phi r_{nt} = 51 \text{ kip}$$

strength reduction factor

$$\Phi := 0.90 \quad B := 24.2 \text{ kip}$$

thickness to prevent prying action

Eq 9-30

$$t_c := \sqrt{\frac{4 \cdot B \cdot b'_{\text{endPL}}}{\Phi \cdot p \cdot F_{u\text{PL}}}} = 1 \text{ in}$$

Eq 9-35

$$\alpha' := \frac{1}{\delta_{\text{endPL}} \cdot (1 + \rho_{\text{endPL}})} \cdot \left[\left(\frac{t_c}{t_{\text{PL}}} \right)^2 - 1 \right] = -0$$

Eq 9-33

$$Q := \left(\frac{t_{\text{PL}}}{t_c} \right)^2 \cdot (1 + \delta_{\text{endPL}} \cdot \alpha') = 1$$

available strength

$$T_{\text{avail}} := B \cdot Q = 24.2 \text{ kip}$$

check capacity

$$\text{if}(r_{\text{ut}} < T_{\text{avail}}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

try $t_{\text{endPL}} = 5/8$ "

$$t_{\text{endPL}} := \frac{5}{8} \text{ in}$$

$$\alpha' := \frac{1}{\delta_{\text{endPL}} \cdot (1 + \rho_{\text{endPL}})} \cdot \left[\left(\frac{t_c}{t_{\text{endPL}}} \right)^2 - 1 \right] = 1.35$$

$$Q := \left(\frac{t_{\text{endPL}}}{t_c} \right)^2 \cdot (1 + \delta_{\text{endPL}}) = 0.66$$

available strength

$$T_{\text{avail}} := B \cdot Q = 16 \text{ kip}$$

check capacity

$$\text{if}(r_{\text{ut}} < T_{\text{avail}}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$\Phi r_{\text{nv}} = 37.9 \text{ kip}$$

$$d_{\text{bolt}} = 0.875 \text{ in}$$

$$t_{\text{endPL}} = 0.625 \text{ in}$$

$$F_{u\text{PL}} = 65 \text{ ksi}$$

Check bolt bearing at bolt holes on end plate (J3.10a)

clear distance

$$l_{c_endPL} := 1.75 \text{ in} - 0.5 \cdot \left(d_{\text{bolt}} + \frac{1}{16} \text{ in} \right) = 1.28 \text{ in}$$

strength reduction factor

$$\Phi := 0.75$$

bolt bearing strength

$$\Phi R_n := \min(\Phi \cdot 1.2 \cdot l_{c_endPL} \cdot t_{\text{endPL}} \cdot F_{u\text{PL}}, \Phi \cdot 2.4 \cdot d_{\text{bolt}} \cdot t_{\text{endPL}} \cdot F_{u\text{PL}}, \Phi r_{\text{nv}}) = 37.9 \text{ kip}$$

check capacity

$$\text{if}(\Phi R_n \geq \Phi r_{\text{nv}}, \text{"bolt shear governs"}, \text{"check bolt bearing"}) = \text{"bolt shear governs"}$$

Check block shear rupture of the end plate (J4.3)recall

block shear strength

$$R_n = 0.60F_u \cdot A_{nv} + U_{bs} \cdot F_u \cdot A_{nt} \leq 0.60F_y \cdot A_{gv} + U_{bs} \cdot F_u \cdot A_{nt}$$

$$V_{\text{column}} = 301.9 \text{ kip}$$

gross shear area (1 side)

$$A_{gv_{\text{endPL}}} := \left[\left(\frac{N_{\text{bolts.end_PL}}}{2} - 1 \right) \cdot p + 1.75 \text{ in} \right] \cdot t_{\text{endPL}} = 12.3 \text{ in}^2$$

$$N_{\text{bolts.end_PL}} = 14$$

$$t_{\text{endPL}} = 0.625 \text{ in}$$

net shear area (1 side)

$$A_{nv_{\text{endPL}}} := A_{gv_{\text{endPL}}} - t_{\text{endPL}} \cdot \left(\frac{N_{\text{bolts.end_PL}}}{2} - 0.5 \right) \cdot \left(d_{\text{bolt}} + \frac{2}{16} \text{ in} \right) = 8.28 \text{ in}^2$$

net tensile area (1 side)

$$A_{nt_{\text{endPL}}} := t_{\text{endPL}} \cdot \left[\frac{h_{\text{endPL}} - \text{gage}}{2} - 0.5 \cdot \left(d_{\text{bolt}} + \frac{2}{16} \text{ in} \right) \right] = 1.09 \text{ in}^2$$

$$0.60F_{u_{\text{PL}}} \cdot A_{nv_{\text{endPL}}} = 323 \text{ kip}$$

$$U_{bs} := 1$$

$$0.60F_{y_{\text{PL}}} \cdot A_{gv_{\text{endPL}}} = 370.3 \text{ kip}$$

strength reduction factor

$$\Phi := 0.75$$

$$U_{bs} \cdot F_{u_{\text{PL}}} \cdot A_{nt_{\text{endPL}}} = 71.1 \text{ kip}$$

block shear strength

$$\Phi R_n := \Phi \cdot (2) \cdot (0.6 \min(F_{u_{\text{PL}}} \cdot A_{nv_{\text{endPL}}}, F_{y_{\text{PL}}} \cdot A_{gv_{\text{endPL}}}) + U_{bs} \cdot F_{u_{\text{PL}}} \cdot A_{nt_{\text{endPL}}}) = 591.1 \text{ kip}$$

check capacity

$$\text{if}(V_{\text{column}} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Check prying action on column flange

$$b_{\text{column}} := \frac{\text{gage} - t_{w_{\text{column}}}}{2} = 2.5 \text{ in}$$

recall

$$\text{gage} = 5.5 \text{ in}$$

$$b'_{\text{column}} := b_{\text{column}} - \frac{d_{\text{bolt}}}{2} = 2.1 \text{ in}$$

$$t_{w_{\text{column}}} = 0.44 \text{ in}$$

$$a_{\text{column}} := \frac{b_{\text{column}} - \text{gage}}{2} = 4.5 \text{ in} \quad \text{use} \quad a_{\text{endPL}} = 2.25 \text{ in}$$

$$d_{\text{bolt}} = 0.875 \text{ in}$$

$$b_{\text{column}} = 14.5 \text{ in}$$

$$a'_{\text{column}} := \min \left(a_{\text{endPL}} + \frac{d_{\text{bolt}}}{2}, 1.25 \cdot b_{\text{column}} + \frac{d_{\text{bolt}}}{2} \right) = 2.69 \text{ in}$$

$$t_{\text{column}} = 0.71 \text{ in}$$

$$p = 3 \text{ in}$$

$$F_{u_{\text{beam}}} = 65 \text{ ksi}$$

$$\rho_{\text{column}} := \frac{b'_{\text{column}}}{a'_{\text{column}}} = 0.78$$

$$r_{ut} = 12.6 \text{ kip}$$

$$\delta_{\text{column}} := 1 - \frac{d'}{p} = 0.69$$

$$\Phi := 0.90$$

$$t_c := \sqrt{\frac{4 \cdot B \cdot b'_{\text{column}}}{\Phi \cdot p \cdot F_{u_{\text{beam}}}}} = 1.074 \text{ in}$$

$$B = 24.2 \text{ kip}$$

$$\alpha' := \frac{1}{\delta_{\text{column}} \cdot (1 + \rho_{\text{column}})} \cdot \left[\left(\frac{t_c}{t_{\text{column}}} \right)^2 - 1 \right] = 1.05$$

$$Q := \left(\frac{t_{\text{column}}}{t_c} \right)^2 \cdot (1 + \delta_{\text{column}}) = 0.74$$

available strength

$$T_{\text{avail}} := B \cdot Q = 17.8 \text{ kip}$$

check capacity

$$\text{if}(r_{ut} < T_{\text{avail}}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

more realistic model

number of bolts in row

$$n := N_{\text{bolts.end_PL}} \div 2 = 7$$

$$a_{\text{bar}} := \frac{b_{\text{fcolumn}} - \text{gage}}{2}$$

$$b_{\text{bar}} := b_{\text{column}} = 2.5 \text{ in}$$

replace p with p.eff

$$p_{\text{eff}} := \frac{(n-1)p + \pi \cdot b_{\text{bar}} + 2 \cdot a_{\text{bar}}}{n} = 5 \text{ in}$$

$$\delta_{\text{column_eff}} := 1 - \frac{d'}{p_{\text{eff}}} = 0.81$$

$$t_{\text{c}} := \sqrt{\frac{4 \cdot B \cdot b'_{\text{column}}}{\Phi \cdot p_{\text{eff}} \cdot F_{\text{Ubeam}}}} = 0.833 \text{ in}$$

$$\alpha' := \frac{1}{\delta_{\text{column_eff}} \cdot (1 + \rho_{\text{column}})} \cdot \left[\left(\frac{t_{\text{c}}}{t_{\text{fcolumn}}} \right)^2 - 1 \right] = 0.26$$

$$Q_{\text{eff}} := \left(\frac{t_{\text{fcolumn}}}{t_{\text{c}}} \right)^2 \cdot (1 + \delta_{\text{endPL}} \cdot \alpha') = 0.86$$

available trength

$$T_{\text{avail.eff}} := B \cdot Q_{\text{eff}} = 20.7 \text{ kip}$$

check capacity

$$\text{if}(r_{\text{ut}} < T_{\text{avail.eff}}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

percent change

$$\frac{T_{\text{avail.eff}} - T_{\text{avail}}}{T_{\text{avail}}} = 16.3\%$$

$$B = 24.2 \text{ kip}$$

Check bearing on column flange

$$t_{\text{fcolumn}} = 0.7 \text{ in} > t_{\text{endPL}} = \frac{5}{8} \text{ in}$$

Beam-to-Column Connection

$$b := \frac{\text{Span}}{2} = 150 \text{ in}$$

$$\text{Height} := \frac{\text{Span}}{\tan(\theta_{\text{brace}})} = 278.1 \text{ in}$$

$$c := \frac{\text{Height}}{2} = 139.1 \text{ in}$$

$$M_{\text{uD}} = 6 \cdot \left(\frac{P}{A \cdot b \cdot c} \right) \left(\frac{l_{\text{b}} \cdot l_{\text{c}}}{\frac{l_{\text{b}}}{b} + \frac{2l_{\text{c}}}{c}} \right) \cdot \left(\frac{b^2 + c^2}{bc} \right)$$

$$M_{\text{uD}} := 6 \cdot \left(\frac{P_{\text{u}}}{A_{\text{gbrace}} \cdot b \cdot c} \right) \left(\frac{I_{\text{xbeam}} \cdot I_{\text{xcolumn}}}{\frac{I_{\text{xbeam}}}{b} + \frac{2I_{\text{xcolumn}}}{c}} \right) \cdot \left(\frac{b^2 + c^2}{b \cdot c} \right)$$

$$M_{\text{uD}} = 1272.8 \text{ in} \cdot \text{kip}$$

recall

$$\text{Span} = 25 \cdot \text{ft}$$

$$\theta_{\text{brace}} = 47.2 \cdot \text{deg}$$

$$I_{\text{xbeam}} = 1830 \text{ in}^4$$

$$I_{\text{xcolumn}} = 999 \text{ in}^4$$

$$A_{\text{gbrace}} = 26.2 \text{ in}^2$$

$$e_{\text{beam}} = 10.7 \text{ in}$$

$$\beta_{\text{bar}} = 12 \text{ in}$$

$$H_{\text{column}} = 176.1 \text{ kip}$$

$$P_{\text{u}} = 840 \text{ kip}$$

$$V_{\text{beam}} = 269.2 \text{ kip}$$

DG 29 EQ 4-12

$$H_{uD} := \frac{M_{uD}}{\beta_{\text{bar}} + e_{\text{beam}}} = 56.1 \text{ kip}$$

$$H_u := H_{\text{column}} - H_{uD} + H_{u_{\text{node}}} = 220 \text{ kip}$$

required shear strength

$$V_u := V_{\text{beam}} + V_{u_{\text{beam}}} = 319.2 \text{ kip}$$

required axial strength

$$T_u := H_u = 220 \text{ kip}$$

Design bolts at beam-to-column connection (J3.6 & J3.7)

number of bolts

$$N_{\text{bolts_beam}} := 12$$

recall

$$\Phi r_{nv} = 37.9 \text{ kip}$$

ultimate shear force per bolt

$$r_{uv} := \frac{V_u}{N_{\text{bolts_beam}}} = 26.6 \text{ kip}$$

$$\Phi r_{nt} = 51 \text{ kip}$$

$$F_{nt_{\text{bolt}}} = 113 \text{ ksi}$$

check capacity

$$\text{if}(r_{uv} < \Phi r_{nv}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

$$F_{nv_{\text{bolt}}} = 84 \text{ ksi}$$

$$A_{\text{bolt}} = 0.6 \text{ in}^2$$

ultimate tensile force per bolt

$$r_{ut} := \frac{T_u}{N_{\text{bolts_beam}}} = 18.3 \text{ kip}$$

$$V_u = 319.2 \text{ kip}$$

$$T_u = 220 \text{ kip}$$

check capacity

$$\text{if}(r_{ut} < \Phi r_{nt}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

strength reduction factor

$$\Phi := 0.75$$

modified nominal tensile stress factored to include shear stress effects

$$F'_{nt} = 1.3 \cdot F_{nt} - \frac{F_{nt}}{\Phi \cdot F_{nv}} \cdot r_{rv} < F_{nt}$$

$$F'_{nt_{\text{bolt}}} := \min \left[1.3 \cdot F_{nt_{\text{bolt}}} - \frac{F_{nt_{\text{bolt}}}}{\Phi \cdot F_{nv_{\text{bolt}}}} \cdot \left(\frac{r_{uv}}{A_{\text{bolt}}} \right), F_{nt_{\text{bolt}}} \right] = 67.6 \text{ ksi}$$

combined loading strength

$$\Phi R_n := \Phi \cdot F'_{nt_{\text{bolt}}} \cdot A_{\text{bolt}} = 30.5 \text{ kip}$$

check capacity

$$\text{if}(r_{ut} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

try Gr 490 bolts

nominal tensile stress

$$F_{nt_{\text{bolt_A490}}} := 113 \text{ ksi}$$

$$\Phi := 0.75 \text{ factored tensile strength per bolt}$$

nominal shear stress

$$F_{nv_{\text{bolt_A490}}} := 84 \text{ ksi}$$

$$B := \Phi \cdot F_{nt_{\text{bolt_A490}}} \cdot A_{\text{bolt}} = 51 \text{ kip}$$

modified nominal tensile stress factored to include shear stress effects

$$F'_{nt_{\text{bolt_A490}}} := \min \left[1.3 \cdot F_{nt_{\text{bolt_A490}}} - \frac{F_{nt_{\text{bolt_A490}}}}{\Phi \cdot F_{nv_{\text{bolt_A490}}}} \cdot \left(\frac{r_{uv}}{A_{\text{bolt}}} \right), F_{nt_{\text{bolt_A490}}} \right] = 67.6 \text{ ksi}$$

strength reduction factor

$$\Phi := 0.75$$

combined loading strength

$$\Phi R_{n_{\text{A490}}} := \Phi \cdot F'_{nt_{\text{bolt_A490}}} \cdot A_{\text{bolt}} = 30.5 \text{ kip}$$

check capacity

$$\text{if}(r_{ut} < \Phi R_{n_{\text{A490}}}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

Design beam web-to-end plate weld (Eq 8-2)

resultant force

$$R_u := \sqrt{V_u^2 + T_u^2} = 387.7 \text{ kip}$$

recall

angle of load

$$\theta_{b_endPL} := \text{atan}\left(\frac{T_u}{V_u}\right) = 34.6 \cdot \text{deg}$$

$$N_{bolts_beam} = 12$$

$$V_u = 319.2 \text{ kip}$$

$$T_u = 220 \text{ kip}$$

effective length of connection

$$l_{b_endPL} := \frac{N_{bolts_beam}}{2} \cdot p$$

end plate weld size

$$D_{b_endPL} := \frac{R_u}{(2) \cdot \left(1.392 \frac{\text{kip}}{\text{in}}\right) \cdot l_{b_endPL} \cdot \left(1.0 + 0.50 \cdot \sin(\theta_{b_endPL})^{1.5}\right)} = 6.4$$

$$D_{b_endPL} := \text{ceil}(D_{b_endPL}) \cdot \text{in} = 7 \text{ in}$$

Check the 5.5in. gage with 7/16in. fillet welds (Table 7-15)

required clearance

$$C_{3_req} := \frac{7}{8} \text{ in}$$

recall

clearance

$$\text{clearance} := \frac{\text{gage}}{2} - \frac{t_{w_beam}}{2} - \frac{D_{b_endPL}}{16} = 2.05 \text{ in}$$

$$t_{w_beam} = 0.515 \text{ in}$$

$$\text{gage} = 5.5 \text{ in}$$

check clearance

$$\text{if}(C_{3_req} < \text{clearance}, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

$$D_{b_endPL} = 7 \text{ in}$$

Check prying action on bolts and end plate (Chapter 9)

beam end plate thickness

$$t_{b_endPL} := \frac{5}{8} \text{ in}$$

recall

$$t_{w_beam} = 0.515 \text{ in}$$

$$b_{beam} := \frac{\text{gage} - t_{w_beam}}{2} = 2.5 \text{ in}$$

$$\text{gage} = 5.5 \text{ in}$$

$$b'_{beam} := b_{beam} - \frac{d_{bolt}}{2} = 2.1 \text{ in}$$

$$d_{bolt} = 0.875 \text{ in}$$

$$h_{endPL} = 10 \text{ in}$$

$$a_{beam} := \frac{h_{endPL} - \text{gage}}{2} = 2.3 \text{ in}$$

$$p = 3 \text{ in}$$

$$F_{uPL} = 65 \text{ ksi}$$

$$a'_{beam} := \min\left(a_{beam} + \frac{d_{bolt}}{2}, 1.25b_{beam} + \frac{d_{bolt}}{2}\right) = 2.7 \text{ in}$$

$$r_{ut} = 18.3 \text{ kip}$$

$$\rho_{b_endPL} := \frac{b'_{beam}}{a'_{beam}} = 0.76$$

$$\delta_{b_endPL} := 1 - \frac{d'}{p} = 0.69$$

$$\Phi := 0.90$$

$$B = 51 \text{ kip}$$

$$t_c := \sqrt{\frac{4 \cdot B \cdot b'_{\text{beam}}}{\Phi \cdot p \cdot F_{u\text{PL}}}} = 1.19 \text{ in}$$

$$B_c := 30.4 \text{ kip}$$

$$\alpha'_{b_end\text{PL}} := \frac{1}{\delta_{b_end\text{PL}} \cdot (1 + \rho_{b_end\text{PL}})} \cdot \left[\left(\frac{t_c}{t_{b_end\text{PL}}} \right)^2 - 1 \right] = 2.2$$

$$Q_{b_end\text{PL}} := \left(\frac{t_{b_end\text{PL}}}{t_c} \right)^2 \cdot (1 + \delta_{b_end\text{PL}}) = 0.46$$

$$T_{\text{avail.}b_end\text{PL}} := B \cdot Q_{b_end\text{PL}} = 14.1 \text{ kip}$$

$$\text{if}(r_{ut} < T_{\text{avail.}b_end\text{PL}}, \text{"OK"} , \text{"NOT OK"}) = \text{"NOT OK"}$$

use thicker plate

$$t_{b_end\text{PL}} := \frac{3}{4} \text{ in}$$

$$\alpha'_{b_end\text{PL}} := \frac{1}{\delta_{b_end\text{PL}} \cdot (1 + \rho_{b_end\text{PL}})} \cdot \left[\left(\frac{t_c}{t_{b_end\text{PL}}} \right)^2 - 1 \right] = 1.3$$

$$Q_{b_end\text{PL}} := \left(\frac{t_{b_end\text{PL}}}{t_c} \right)^2 \cdot (1 + \delta_{b_end\text{PL}}) = 0.67$$

available strength

$$T_{\text{avail.}b_end\text{PL}} := B \cdot Q_{b_end\text{PL}} = 20.3 \text{ kip}$$

check capacity

$$\text{if}(r_{ut} < T_{\text{avail.}b_end\text{PL}}, \text{"OK"} , \text{"NOT OK"}) = \text{"OK"}$$

Check prying action on column flange

$$t_c := \sqrt{\frac{4 \cdot B \cdot b'_{\text{column}}}{\Phi \cdot p \cdot F_{u\text{beam}}}} = 1.2 \text{ in}$$

recall

$$b'_{\text{column}} = 2.09 \text{ in}$$

$$a'_{\text{column}} = 2.7 \text{ in}$$

$$\rho_{\text{column}} = 0.8$$

$$p = 3 \text{ in}$$

$$\delta_{\text{column}} = 0.688$$

$$F_{u\text{beam}} = 65 \text{ ksi}$$

$$t_{f\text{column}} = 0.7 \text{ in}$$

$$r_{ut} = 18.3 \text{ kip}$$

$$B = 30.4 \text{ kip}$$

$$\alpha'_{\text{column}} := \frac{1}{\delta_{\text{column}} \cdot (1 + \rho_{\text{column}})} \cdot \left[\left(\frac{t_c}{t_{f\text{column}}} \right)^2 - 1 \right] = 1.5$$

$$Q_{\text{column}} := \left(\frac{t_{f\text{column}}}{t_c} \right)^2 \cdot (1 + \delta_{\text{column}} \cdot 1) = 0.59$$

$$T_{\text{avail.}column} := B \cdot Q_{\text{column}} = 17.8 \text{ kip}$$

$$\text{if}(r_{ut} < T_{\text{avail.}column}, \text{"OK"} , \text{"NOT OK"}) = \text{"NOT OK"}$$

Check bolt bearing at end plateCheck block shear rupture on end plate (J4.3)

block shear strength

$$R_n = 0.60F_u \cdot A_{nv} + U_{bs} \cdot F_u \cdot A_{nt} \leq 0.60F_y \cdot A_{gv} + U_{bs} \cdot F_u \cdot A_{nt}$$

gross area in shear (1 side)

$$A_{gv_{b_endPL}} := \left[\left(\frac{N_{bolts_beam}}{2} - 1 \right) \cdot p + 4.40 \text{ in} \right] \cdot t_{b_endPL}$$

$$A_{gv_{b_endPL}} = 14.5 \text{ in}^2$$

net shear area (1 side)

$$A_{nv_{b_endPL}} := A_{gv_{b_endPL}} - t_{b_endPL} \cdot \left[\left(\frac{N_{bolts_beam}}{2} - 0.5 \right) \cdot \left(d_{bolt} + \frac{2}{16} \text{ in} \right) \right] = 10.4 \text{ in}^2$$

net tensile area (1 side)

$$A_{nt_{b_endPL}} := t_{b_endPL} \cdot \left[\frac{h_{endPL} - \text{gage}}{2} - 0.5 \cdot \left(d_{bolt} + \frac{2}{16} \text{ in} \right) \right] = 1.31 \text{ in}^2$$

$$0.60F_{u_{PL}} \cdot A_{nv_{b_endPL}} = 406.6 \text{ kip}$$

$$0.60F_{y_{PL}} \cdot A_{gv_{b_endPL}} = 436.5 \text{ kip}$$

$$U_{bs} \cdot F_{u_{PL}} \cdot A_{nt_{b_endPL}} = 85.3 \text{ kip}$$

strength reduction factor

$$\Phi := 0.75$$

block shear strength

$$\Phi R_n := \Phi \cdot (2) \cdot (0.6 \min(F_{u_{PL}} \cdot A_{nv_{b_endPL}}, F_{y_{PL}} \cdot A_{gv_{b_endPL}}) + U_{bs} \cdot F_{u_{PL}} \cdot A_{nt_{b_endPL}})$$

$$\Phi R_n = 737.8 \text{ kip}$$

check capacity

$$\text{if}(V_u < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$h_{endPL} = 10 \text{ in}$$

$$t_{b_endPL} = 0.8 \text{ in}$$

$$N_{bolts_beam} = 12$$

$$d_{bolt} = 0.875 \text{ in}$$

$$\text{gage} = 5.5 \text{ in}$$

recall

$$V_u = 319.2 \text{ kip}$$

Check beam shear strength (J4.2)

gross shear area

$$A_{gv_{beam}} := d_{beam} \cdot t_{w_{beam}} = 11 \text{ in}^2$$

strength reduction factor

$$\Phi := 1.00$$

shear strength

$$\Phi R_n := \Phi \cdot 0.60 \cdot F_{y_{beam}} \cdot A_{gv_{beam}} = 330.6 \text{ kip}$$

check capacity

$$\text{if}(V_u < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$d_{beam} = 21.4 \text{ in}$$

$$t_{w_{beam}} = 0.515 \text{ in}$$

$$F_{y_{beam}} = 50 \text{ ksi}$$

$$V_u = 319.2 \text{ kip}$$

Check column shear strength (J4.2)

gross shear area

$$A_{gv_{column}} := d_{column} \cdot t_{w_{column}} = 6.2 \text{ in}^2$$

strength reduction factor

$$\Phi := 1.00$$

shear strength

$$\Phi R_n := \Phi \cdot 0.60 \cdot F_{y_{beam}} \cdot A_{gv_{column}} = 184.8 \text{ kip}$$

check capacity

$$\text{if}(H_{column} < \Phi R_n, \text{"OK"}, \text{"NOT OK"}) = \text{"OK"}$$

recall

$$d_{column} = 14 \text{ in}$$

$$t_{w_{column}} = 0.44 \text{ in}$$

$$F_{y_{beam}} = 50 \text{ ksi}$$

$$H_{column} = 176.1 \text{ kip}$$